# Annexe A: New/Revised Course Content in OBTL+ Format

## **Course Overview**

The sections shown on this interface are based on the templates UG OBTL+ or PG OBTL+

If you are revising/duplicating an existing course and do not see the pre-filled contents you expect in the subsequent sections e.g. Course Aims, Intended Learning Outcomes etc. please refer to Data Transformation Status for more information.

| Expected Implementation in Academic Year                   | AY2024-2025                             |
|--|---|
| Semester/Trimester/Others (specify approx. Start/End date) | Semester 2                              |
| Course Author<br>* Faculty proposing/revising the course   | Pui Tze Sian                            |
| Course Author Email  | tspui@ntu.edu.sg, Tej.choksi@ntu.edu.sg |
| Course Title   | Engineering Mathematics                 |
| Course Code  | CB1117                                  |
| Academic Units   | 4                                       |
| Contact Hours  | 52                                      |
| Research Experience Components                             | Not Applicable                          |

## **Course Requisites (if applicable)**

| Pre-requisites           | MH1810 Mathematics |
|--------------------------|--------------------|
| Co-requisites            |                    |
| Pre-requisite to         |                    |
| Mutually exclusive to    |                    |
| Replacement course<br>to |                    |
| Remarks (if any)         |                    |

## **Course Aims**

This course serves as a foundation course on engineering mathematics. It covers a broad range of fundamental topics, including Differential Equations, Linear Algebra, Vector Calculus, Probability and Mathematical Statistics. These key concepts will be important and useful to those of you who are pursuing Engineering studies, with applications in modelling and solutions of systems.

## **Course's Intended Learning Outcomes (ILOs)**

Upon the successful completion of this course, you (student) would be able to:

| ILO 1 | Describe and apply ODE models towards simple systems.   |
|-------|---|
| ILO 2 | Solve first and second order ODE problems, including Laplace transform or linear algebraic methods. |
| ILO 3 | Recognize PDE models and integrate functions of several variables over curves and surfaces          |
| ILO 4 | Understand how to differentiate and integrate multi-variate functions.                              |
| ILO 5 | Learn the basics of vector operations relevant to applications in engineering.                      |

## **Course Content**

1. Model a simple system to obtain a first order ODE. 2. Solve linear and nonlinear first order ODEs as well as the second order linear homogeneous and nonhomogeneous ODE 3. Solve initial value problems using the Laplace transform. 4. Calculate determinant and matrix inverse of higher order matrices. 5. Solve a system of linear algebraic equations using Laplace transform. 6. Calculate eigenvalues and eigenvectors 7. Use eigenvalues and eigenvectors to solve the 1st order linear systems 8. Apply partial derivatives to evaluate directional derivatives, gradient vectors, tangent planes, etc. 9. Determine the extrema of functions of multiple variables and apply it to different practical maximization/minimization problems. 10. Apply multiple integral to evaluate areas, volumes, etc. 11. Perform line integral and surface integral over given curves and surfaces. 12. Use Fourier series to represent any periodic function 13. Apply the method of separation of variables to solve 1D heat equations 14. Apply probability theory and basic mathematical statistics

# Reading and References (if applicable)

- 1. Erwin Kreyszig, Advanced Engineering Mathematics, 10th edition, John Wiley & Sons, 2010.
- 2. Thomas, George Brinton, et al. Thomas' Calculus, 14th Edition, Pearson, 2017.

# **Planned Schedule**

| Week<br>or<br>Session | Topics or Themes   | ILO | Readings              | Delivery Mode | Activities                            |
|-----------------------|--|-----|-----------------------|---------------|---------------------------------------|
| 1                     | Modelling Linear<br>And Nonlinear<br>1st Order ODE                     | 1   | Reading list [1], [2] | In-person     | Face to face<br>lecture               |
| 2                     | 2nd Order ODE:<br>Linear<br>Homogeneous<br>And<br>Applications         | 1,2 | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 1 |
| 3                     | 2nd Order ODE:<br>Linear<br>Nonhomogeneo<br>us And<br>Applications     | 2   | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 2 |
| 4                     | Laplace<br>Transforms,<br>Heaviside<br>Function                        | 2   | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 3 |
| 5                     | Laplace<br>Transforms,<br>Heaviside<br>Function                        | 2   | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 4 |
| 6                     | Linear Algebra<br>And<br>Eigenvalues/Eig<br>envectors                  | 2   | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 5 |
| 7                     | System Of The<br>First Order<br>Linear ODE                             | 2   | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 6 |
| 8                     | Introduction to<br>dimensional<br>coordinate<br>geometry               | 3   | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 7 |
| 9                     | Introduction to<br>multivariable<br>functions, partial<br>differential | 4   | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 8 |

| Week<br>or<br>Session | Topics or Themes  | ILO | Readings              | Delivery Mode | Activities                             |
|-----------------------|---|-----|-----------------------|---------------|--|
| 10                    | Directional<br>derivatives,<br>gradients,<br>double integrals     | 4   | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 9  |
| 11                    | Area, volume,<br>and probability<br>through multiple<br>integrals | 5   | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 10 |
| 12                    | Line integrals<br>and Vector<br>Fields, potential<br>functions    | 5   | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 11 |
| 13                    | Green's<br>theorem,<br>surface area and<br>surface<br>integrals.  | 5   | Reading list [1], [2] | In-person     | Face to face<br>lecture<br>Tutorial 12 |

# Learning and Teaching Approach

| Approach     | How does this approach support you in achieving the learning outcomes?  |
|--------------|---|
| Lectur<br>e  | Demonstrate how to carry out a procedure such as working through a problem, use incomplete handouts which enabling students participating in class. |
| Tutoria<br>I | Class room discussion sessions on tutorial questions and related topics   |

## **Assessment Structure**

Assessment Components (includes both continuous and summative assessment)

| No. | Component   | ILO       | Related PLO or<br>Accreditation | Weightage | Team/Individual | Rubrics  | Level of<br>Understanding |
|-----|---|-----------|---------------------------------|-----------|-----------------|----------|---------------------------|
| 1   | Continuous Assessment<br>(CA): Test/Quiz()              | 1, 2      | EAB, SLO, a, b,<br>c            | 20        | Individual      | Analytic | Multistructural           |
| 2   | Continuous Assessment<br>(CA): Test/Quiz()              | 4         | EAB, SLO, a, b,<br>c            | 17        | Individual      | Analytic | Multistructural           |
| 3   | Continuous Assessment<br>(CA): Class<br>Participation() | 4,5       | EAB, SLO, a, b,<br>c            | 3         | Individual      | Analytic | Multistructural           |
| 4   | Summative Assessment<br>(EXAM): Final exam()            | 1,2,3,4,5 | EAB, SLO, a, b,<br>c            | 60        | Individual      | Analytic | Relational                |

Description of Assessment Components (if applicable)

## Formative Feedback

Examination results;

Marker's report on overall examination performance will be uploaded to NTUlearn;

Quiz answers will be discussed in class

## NTU Graduate Attributes/Competency Mapping

This course intends to develop the following graduate attributes and competencies (maximum 5 most relevant)

| Attributes/Competency | Level        |
|-----------------------|--------------|
| Creative Thinking     | Basic        |
| Curiosity             | Intermediate |
| Problem Solving       | Basic        |

# **Course Policy**

## Policy (Academic Integrity)

Good academic work depends on honesty and ethical behaviour. The quality of your work as a student relies on adhering to the principles of academic integrity and to the NTU Honour Code, a set of values shared by the whole university community. Truth, Trust and Justice are at the core of NTU's shared values. As a student, it is important that you recognize your responsibilities in understanding and applying the principles of academic integrity in all the work you do at NTU. Not knowing what is involved in maintaining academic integrity does not excuse academic dishonesty. You need to actively equip yourself with strategies to avoid all forms of academic dishonesty, including plagiarism, academic fraud, collusion and cheating. If you are uncertain of the definitions of any of these terms, you should go to the academic integrity website for more information. On the use of technological tools (such as Generative AI tools), different courses / assignments have different intended learning outcomes. Students should refer to the specific assignment instructions on their use and requirements and/or consult your instructors on how you can use these tools to help your learning. Consult your instructor(s) if you need any clarification about the requirements of academic integrity in the course.

## Policy (General)

General: Students are expected to complete all online activities and take all scheduled assignments and tests by due dates. Students are expected to take responsibility to follow up with course notes, assignments and course related announcements. Students are expected to participate in all tutorial discussions and activities.

#### Policy (Absenteeism)

Continuous assessments: Students are required to attend all continuous assessments. Absenteeism: Continuous assessments make up a significant portion of students' course grade. Absence from continuous assessments without officially approved leave will result in no marks and affect students' overall course grade.

#### Policy (Others, if applicable)

ssments without officially approved leave will result in no marks and affect students' overall course grade.

## Last Updated Date: 27-03-2024 01:59:03

Last Updated By: Raymond Lau Wai Man (Assoc Prof)

#### Appendix : Rubric/Assessment Criteria for Components listed in Assessment Table

#### Appendix 1: Assessment Criteria

| Criteria  | Unsatisfactory:<br><u>&lt;40%</u>  | Borderline: 40%<br>to 49%   | Satisfactory: 50%<br>to 69%   | <u>Very good: 70%</u><br><u>to 89%</u>   | Exemplary: >90%  |
|---|--|---|---|--|--|
| Knowledge<br>Understandin<br>g general vs<br>particular<br>solution                           | <ul> <li>Lacks<br/>understandin<br/>g of theories,<br/>concepts, and<br/>terms<br/>governing 1<sup>st</sup><br/>and 2<sup>nd</sup> ODE.</li> </ul> | <ul> <li>Partial<br/>understandin<br/>g of theories,<br/>concepts, and<br/>terms<br/>governing 1<sup>st</sup><br/>and 2<sup>nd</sup> ODE</li> </ul> | • Good<br>understandin<br>g of the<br>theories,<br>concepts, and<br>terms<br>governing 1 <sup>st</sup><br>and 2 <sup>nd</sup> ODE | Good and<br>comprehensi<br>ve<br>understandin<br>g of the<br>theories,<br>concepts, and<br>terms<br>governing 1 <sup>st</sup><br>and 2 <sup>nd</sup> ODE | <ul> <li>Very good<br/>and<br/>comprehensi<br/>ve<br/>understandin<br/>g of theories,<br/>concepts, and<br/>terms<br/>governing 1<sup>st</sup><br/>and 2<sup>nd</sup> ODE</li> </ul> |
| Analysis<br>The ability to<br>comprehend<br>2 <sup>nd</sup> order and<br>higher order<br>ODEs | <ul> <li>Unable to<br/>apply the<br/>theories and<br/>concepts to<br/>solve 1<sup>st</sup> and<br/>2<sup>nd</sup> ODEs<br/>problems</li> </ul>     | Can apply<br>the theories<br>and concepts<br>to solve<br>simple 1 <sup>st</sup><br>and 2 <sup>nd</sup><br>ODEs<br>problem                           | Can apply<br>the theories<br>and concepts<br>to solve<br>medium<br>level 1 <sup>st</sup> and<br>2 <sup>nd</sup> ODEs<br>problem   | Can apply<br>the theories<br>and concepts<br>to solve<br>complicated<br>1 <sup>st</sup> and 2 <sup>nd</sup><br>ODEs<br>problem                           | <ul> <li>Can apply<br/>the theories<br/>and concepts<br/>to solve 1<sup>st</sup>,<br/>2<sup>nd</sup> and<br/>higher order<br/>ODEs<br/>problem.</li> </ul>                           |

## Appendix 2: Assessment Criteria

| Criteria     | Unsatisfactory: <40%               | Pass: 40% to 69%              | High Standard: >70%               |
|--------------|------------------------------------|-------------------------------|-----------------------------------|
| Method of    | Using methods that are irrelevant  | Able to identify relevant     | Applying methods and theorems     |
| approach     | or do not apply to the given       | methods that help solve the   | that are relevant and efficiently |
| (40%)        | problem.                           | problem but unable to arrive  | to solve the entire problem.      |
|              | Applying theorems whose            | at the complete / appropriate |                                   |
|              | conditions are not satisfied.      | solution.                     |                                   |
| Validity of  | The student's reasoning is         | The student's reasoning is    | The student's reasoning is        |
| reasoning    | logically invalid.                 | logically valid               | logically valid and effective     |
| (40%)        |                                    |                               |                                   |
| Presentation | The student's argument is poorly   | The student's argument is     | The student's argument is clear,  |
| of answer    | explained or not explained at all. | clear, but may contain some   | precise, with no or insignificant |
| (20%)        |                                    | gaps.                         | gaps.                             |

#### Appendix 3: Assessment Criteria

Class participation will be gauged by weekly online polls. These polls serve as a selfassessment tool for the student, and help the faculty gauge the pulse of the class in terms of effectiveness of the learning. Points are awarded for participation, regardless of whether the answers are correct/wrong.

| Criteria             | Grade                    |
|----------------------|--------------------------|
| Answers 5 or 6 of    | 3% (Full                 |
| the 6 polls          | points)                  |
| Answer 3 or 4 of the | 1% (1/3 <sup>rd</sup> of |
| 6 polls              | the points)              |
| Answer 0, 1, or 2 of | 0% (0 points)            |
| the 6 polls          |                          |

| A | opendix | 4: | Assessment | Criteria | Final | Exam |
|---|---------|----|------------|----------|-------|------|
|---|---------|----|------------|----------|-------|------|

| Criteria  | <u>Unsatisfactory:</u><br><40%   | Borderline: 40%<br>to 49%   | Satisfactory: 50% to<br>69%  | <u>Very good: 70% to</u><br><u>89%</u>  | Exemplary: >90%  |  |
|---|--|---|--|---|--|--|
| Knowledge<br>Understanding<br>general vs particular<br>solution.                                  | <ul> <li>Lacks<br/>understandin<br/>g of theories,<br/>concepts, and<br/>terms<br/>governing 1<sup>st</sup><br/>and 2<sup>nd</sup> ODE.</li> </ul> | <ul> <li>Partial<br/>understandin<br/>g of theories,<br/>concepts, and<br/>terms<br/>governing 1<sup>st</sup><br/>and 2<sup>nd</sup> ODE</li> </ul> | • Good<br>understanding<br>of the theories,<br>concepts, and<br>terms<br>governing 1 <sup>st</sup><br>and 2 <sup>nd</sup> ODE                              | Good and<br>comprehensive<br>understanding of<br>the theories,<br>concepts, and terms<br>governing 1 <sup>st</sup> and<br>2 <sup>nd</sup> ODE | <ul> <li>Very good<br/>and<br/>comprehensi<br/>ve<br/>understandin<br/>g of theories,<br/>concepts, and<br/>terms<br/>governing 1<sup>st</sup><br/>and 2<sup>nd</sup> ODE</li> </ul> |  |
| <u>Analysis</u><br>The ability to<br>comprehend 2 <sup>nd</sup><br>order and higher<br>order ODEs | • Unable to<br>apply the<br>theories and<br>concepts to<br>solve 1 <sup>st</sup> and<br>2 <sup>nd</sup> ODEs<br>problems                           | <ul> <li>Can apply the<br/>theories and<br/>concepts to<br/>solve simple 1<sup>st</sup><br/>and 2<sup>nd</sup> ODEs<br/>problem</li> </ul>          | <ul> <li>Can apply the<br/>theories and<br/>concepts to solve<br/>medium level 1<sup>st</sup><br/>and 2<sup>nd</sup> ODEs<br/>problem</li> </ul>           | <ul> <li>Can apply the<br/>theories and<br/>concepts to solve<br/>complicated 1<sup>st</sup> and<br/>2<sup>nd</sup> ODEs problem</li> </ul>   | <ul> <li>Can apply the<br/>theories and<br/>concepts to<br/>solve 1<sup>st</sup>, 2<sup>nd</sup><br/>and higher<br/>order ODEs<br/>problem.</li> </ul>                               |  |
| Method of approach  | <ul> <li>Unable to<br/>apply<br/>appropriate<br/>methods to<br/>analyze<br/>mathematical<br/>problems<br/>effectively.</li> </ul>                  | Can apply<br>some methods<br>to analyze<br>simple<br>mathematical<br>problems.  | <ul> <li>Can apply<br/>various methods<br/>to analyze<br/>medium level<br/>mathematical<br/>problems.</li> </ul>   | <ul> <li>Can apply<br/>advanced methods<br/>to analyze complex<br/>mathematical<br/>problems.</li> </ul>                                      | <ul> <li>Can apply<br/>advanced<br/>methods to<br/>analyze all<br/>types of<br/>mathematical<br/>problems<br/>proficiently.</li> </ul>   |  |
| <u>Validity of</u><br><u>reasoning</u>  | The student's<br>reasoning is<br>logically<br>invalid,<br>leading to<br>incorrect<br>conclusions<br>or solutions.                                  | • The student's<br>reasoning is<br>logically valid<br>but may lack<br>clarity or<br>completeness in<br>some aspects.                                | <ul> <li>The student's<br/>reasoning is<br/>logically valid<br/>and adequately<br/>supports the<br/>conclusions or<br/>solutions<br/>presented.</li> </ul> | • The student's<br>reasoning is<br>logically valid<br>and effectively<br>supports the<br>conclusions or<br>solutions<br>presented.            | The student's<br>reasoning is<br>logically<br>valid, precise,<br>and<br>demonstrates<br>exceptional<br>clarity and<br>effectiveness<br>in supporting<br>conclusions or<br>solutions. |  |

## Mapping of Course ILOs to EAB Graduate Attributes

| Course Code & Title | CB 1117 & Engineering Mathematics |
|---------------------|-----------------------------------|
| Course Type         | Core                              |

| Overview  |    |     |   |     |   |     |     |     |  |
|---|----|-----|---|-----|---|-----|-----|-----|--|
| (a)   | •  | (b) | • | (c) | • | (d) | (e) | (f) |  |
| (g)   |    | (h) |   | (i) |   | (j) | (k) |     |  |
| Legend  | d: |     |   |     |   |     |     |     |  |
| <ul> <li>Fully consistent (contributes to more than 75% of Student Learning Outcome)</li> </ul> |    |     |   |     |   |     |     |     |  |
| <ul> <li>Partially consistent (contributes to about 50% of Student Learning Outcome)</li> </ul> |    |     |   |     |   |     |     |     |  |
| O Weakly consistent (contributes to about 25% of Student Learning Outcome)                      |    |     |   |     |   |     |     |     |  |
| Blank Not related to Student Learning Outcome   |    |     |   |     |   |     |     |     |  |

|     | Course ILOs  | EAB Graduate Attributes |  |  |  |
|-----|--|-------------------------|--|--|--|
| 1)  | Describe and apply ODE models towards simple systems.  | a,b                     |  |  |  |
| 2)  | Solve first and second order ODE problems, including<br>Laplace transform or linear algebraic methods. | b, c                    |  |  |  |
| 3)  | Recognize PDE models and integrate functions of several variables over curves and surfaces             | a, b                    |  |  |  |
| 4)  | Understand how to differentiate and integrate multi-<br>variate functions.                             | b, c                    |  |  |  |
| 5)  | Learn the basics of vector operations relevant to applications in engineering.                         | b, c                    |  |  |  |
| 6)  |  |                         |  |  |  |
| 7)  |  |                         |  |  |  |
| 8)  |  |                         |  |  |  |
| 9)  |  |                         |  |  |  |
| 10) |  |                         |  |  |  |

## EAB Graduate Attributes

- a) **Engineering Knowledge**: Apply the knowledge of mathematics, natural science, computing and engineering fundamentals, and an engineering specialisation as specified in WK1 to WK4 respectively to the solution of complex engineering problems.
- b) Problem Analysis: Identify, formulate, research literature, and analyse complex engineering problems reaching substantiated conclusions using first principles of mathematics, natural sciences, and engineering sciences with holistic considerations for sustainable development. (WK1 to WK4)
- c) **Design / Development of Solutions**: Design creative solutions for complex engineering problems and design systems, components or processes that meet identified needs with appropriate consideration for public health and safety, whole-life cost, net zero carbon as well as resource, cultural, societal, and environmental considerations as required. (WK5)
- d) **Investigation**: Conduct investigations of complex problems using research-based knowledge (WK8) and research methods including design of experiments, analysis and interpretation of data, and synthesis of the information to provide valid conclusions.
- e) **Modern Tool Usage**: Create, select and apply appropriate techniques, resources, and modern engineering and IT tools including prediction and modelling to complex engineering problems, with an understanding of the limitations. (WK2 and WK6)
- f) **The Engineer and the World**: When solving complex engineering problems, analyse and evaluate sustainable development impacts to: society, the economy, sustainability, health and safety, legal frameworks and the environment (WK1, WK5, and WK7).
- g) **Ethics**: Apply ethical principles and commit to professional ethics and responsibilities and norms of engineering practice and adhere to relevant national and international laws. Demonstrate an understanding of the need for diversity and inclusion (WK9).
- h) **Individual and Collaborative Team Work**: Function effectively as an individual, and as a member or leader in diverse and inclusive teams and in multidisciplinary, face-to-face, remote and distributed settings (WK9).
- i) **Communication**: Communicate effectively and inclusively on complex engineering activities with the engineering community and with society at large, such as being able to comprehend and write effective reports and design documentation, make effective presentations, and give and receive clear instructions, taking into account cultural, language, and learning differences.
- j) Project Management and Finance: Demonstrate knowledge and understanding of engineering management principles and economic decision-making, and apply these to one's own work, as a member and leader in a team, to manage projects and in multidisciplinary environments.
- k) Life-long Learning: Recognise the need for, and have the preparation and ability to (i) engage in independent and life-long learning, and (ii) adapt to new and emerging technologies, and (iii) think critically, in the broadest context of technological change (WK8).

| No  | Knowledge Profile  |
|-----|--|
| WK1 | A systematic, theory-based understanding of the natural sciences applicable to the discipline and awareness of relevant social sciences  |
| WK2 | Conceptually-based mathematics, numerical analysis, data analysis, statistics<br>and formal aspects of computer and information science to support detailed<br>analysis and modelling applicable to the discipline                                     |
| WK3 | A systematic, theory-based formulation of engineering fundamentals required in the engineering discipline  |
| WK4 | Engineering specialist knowledge that provides theoretical frameworks and<br>bodies of knowledge for the accepted practice areas in the engineering<br>discipline; much is at the forefront of the discipline  |
| WK5 | Knowledge including efficient resource use, environmental impacts, whole-life cost, re-use of resources, net zero carbon, and similar concepts that supports engineering design and operations in a practice area                                      |
| WK6 | Knowledge of engineering practice (technology) in the practice areas in the engineering discipline   |
| WK7 | Knowledge of the role of engineering in society and identified issues in<br>engineering practice in the discipline such as the professional responsibility of<br>an engineer to public safety and sustainable development.                             |
| WK8 | Engagement with selected knowledge in the current research literature of the discipline, awareness of the power of critical thinking and creative approaches to evaluate emerging issues   |
| WK9 | Knowledge of professional ethics, responsibilities, and norms of engineering practice. Awareness of the need for diversity by reason of ethnicity, gender, age, physical ability etc with mutual understanding and respect, and of inclusive attitudes |

Reference: EAB Accreditation Manual